

## Lahar Flow Models

References:

*Encyclopedia of Volcanoes*: pp 601-616

Scott, KM, 1988, Origins, behavior, and sedimentology of lahars and lahar-runout flows in the Toutle-Cowlitz River system: USGS Prof. Paper 1447A.

Iverson, RM, 1997, The physics of Debris flows, *Reviews of Geophysics*, **35**:245-296

## Model Constraints

- Flows are neither steady nor uniform
- Pore pressure is laterally heterogeneous
- Mobility governed by fluid interiors with lithostatic pore pressures and resistant coarse-grained exteriors
- There is a range from frictional to collisional grain interactions

## Flow Resistance

- Bingham model
  - Assumes a rigid plug
- Bagnold model
  - Assumes grain collisions
- Combination model
  - Coulomb friction plus collisional losses

## Shear Strength

- ①  $k = c + \sigma \tan \phi$ 
  - $k$  = shear strength
  - $c$  = cohesion
  - $\sigma$  = normal stress
  - $\phi$  = friction angle
- ②  $\sigma = (\sigma - P)$ 
  - $P$  = pore pressure

## Bingham Model

- Describes movement of clay slurries
- A rigid plug is inferred
- Resistance depends on viscosity ( $\mu$ ) and strength ( $S$ ) of the material

$$\tau_b = S + \mu \, du/dt$$

## Bagnold Model

- Assumes that grain collisions are important
- Resisting stress in granular flow is given by:

$$\tau_b = v \rho_s d^2 (du/dt)^2$$

$v$  is the solids fraction

$d$  is the particle diameter

$\rho_s$  is the density of solid particles

$d^2 (du/dt)^2$  is proportional to the granular temperature

## Combination Model

- Both Coulomb friction and collisional losses
- Movement in a viscous fluid

$$\tau_f = v (\rho_s g h - P) \tan(\varphi)$$

$\tan(\varphi)$  is the friction coefficient

$P$  is the fluid pressure

- If  $P = \rho_s g h$  the flow is liquefied
- At the flow perimeter  $P = \rho_f g h$
- In the flow interior,  $P = 0.8 \rho_s g h$

## Flow Components

- Fluid phase
  - Frictionless mixture water and fine particles
  - Responsible for cohesive strength
- Granular phase
  - Coarser particles
  - Determines frictional strength

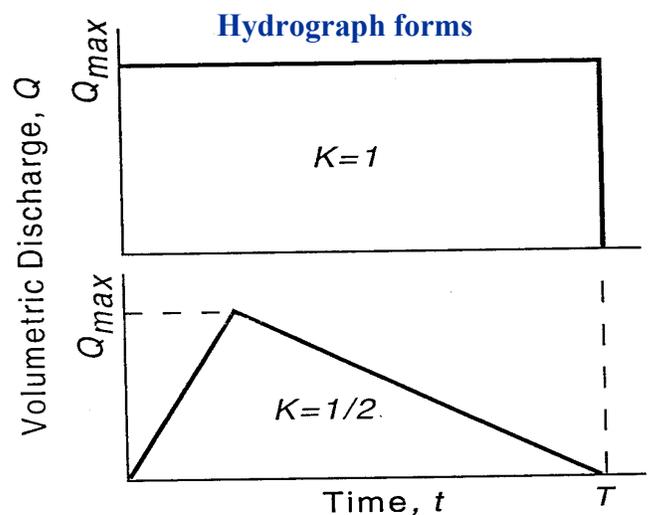
## Flow Transformations

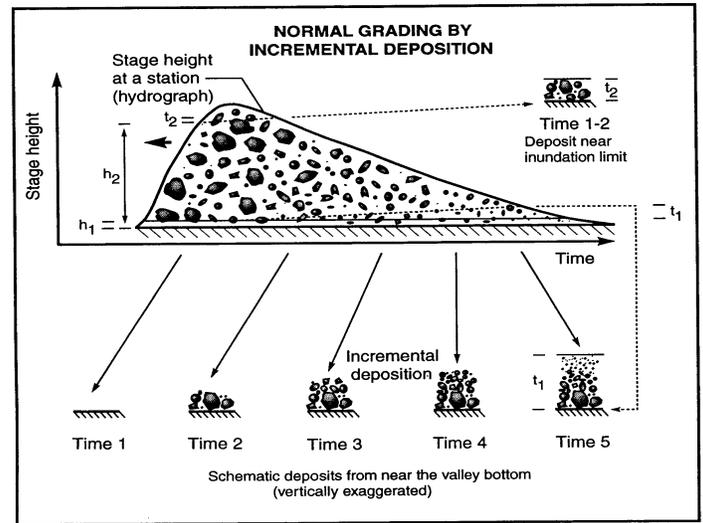
- Debris avalanches
- Debris flows
- Hyperconcentrated flows
- Stream flows



## Hydrograph

- Flow characteristics vs. time
- Stage height (m)
- Discharge
  - $Q$  ( $m^3/s$ )
  - Area under the curve is total volume
- Maximum discharge
- Duration





## Geometric Considerations

- Source
  - Size and shape
  - volume
- Deposit
  - Cross sectional area
  - Planimetric area

## Source Characteristics

- General failure body
- Saucer shaped geometry
- Terzaghi (1931) slip surface
- Volume approximation
  - cone formula
  - volume  $\sim 1/3 \pi r^2 h \sim A h/3$

## Method of Slices

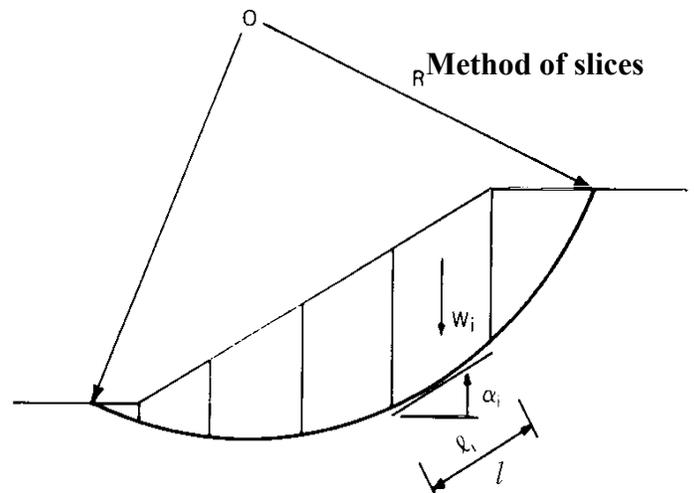
$$F = (\sum S_{ui} l) / (\sum W_i \sin \alpha_i)$$

$S_u$  = undrained shear strength

$l$  = length of arc

$W$  = weight of slice

$\alpha$  = slope angle of slice



## LAHARZ Model

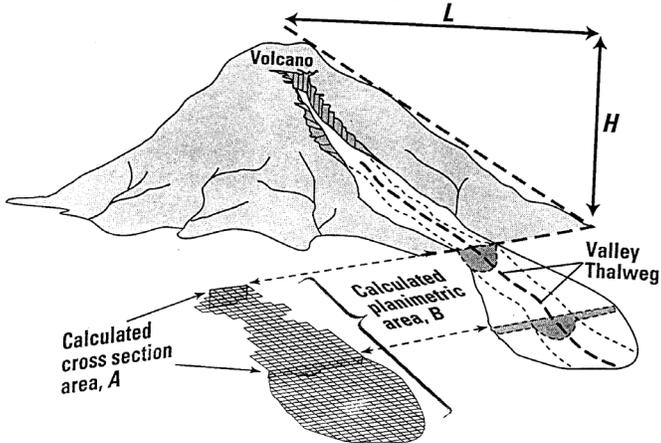
Reference:

Iverson, Richard M., Schilling, Steven P., Vallance, James W., 1998, Objective delineation of lahar-inundation hazard zones, Geological Society of America Bulletin, 110 (8), p. 972-984.

## Deposit Geometry

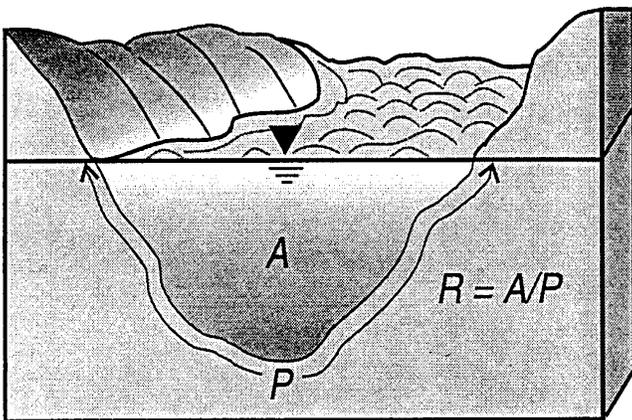
- Cross sectional area ( $A_{sec}$ )
  - Stream profile
  - Top of deposit/flow
- Planimetric area ( $A_{sur}$ )
  - Outline of deposit
- Cumulative volume calculation

### Model to calculate flow volumes



## Calculation of Areas

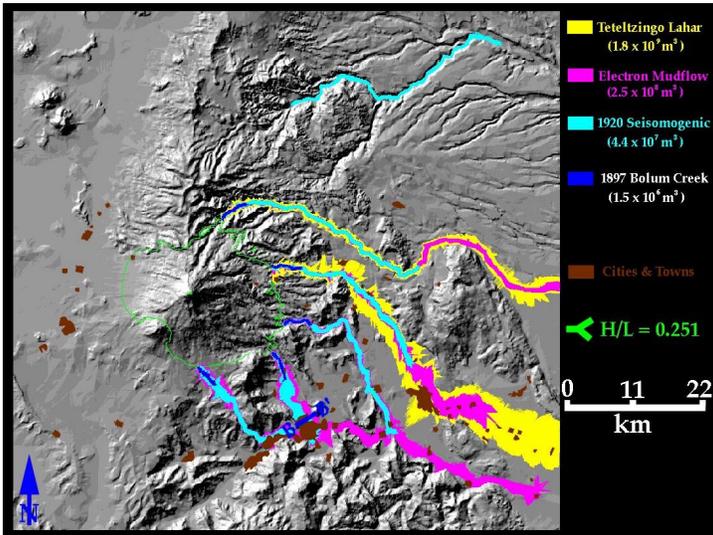
- Model of Iverson et al. (1998)
- Sectional Area
 
$$A = 0.05 V^{2/3}$$
- Planimetric Area
 
$$B = 200 V^{2/3}$$
- Volumes are incrementally deposited



**Hydraulic radius (R) = Wetted perimeter \* Area**

## Pico de Orizaba

- Many large debris flows have occurred in the past
- Several orders of magnitude modeled with LAHARZ
- This is the basis of a debris-flow hazards map of the volcano



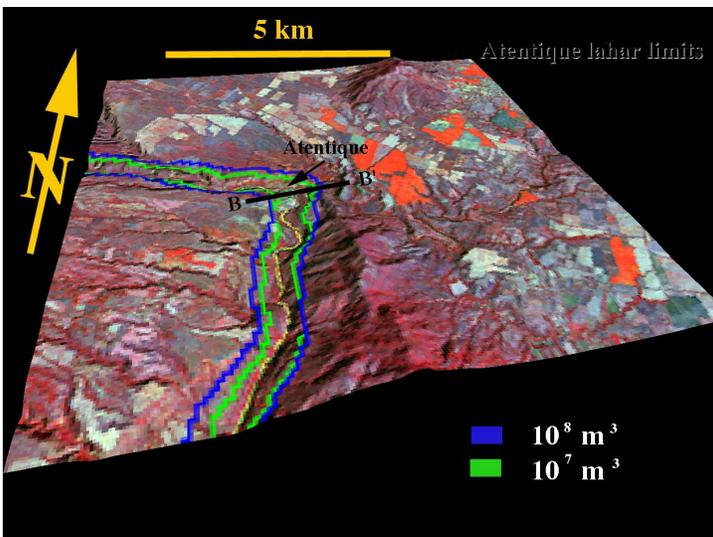
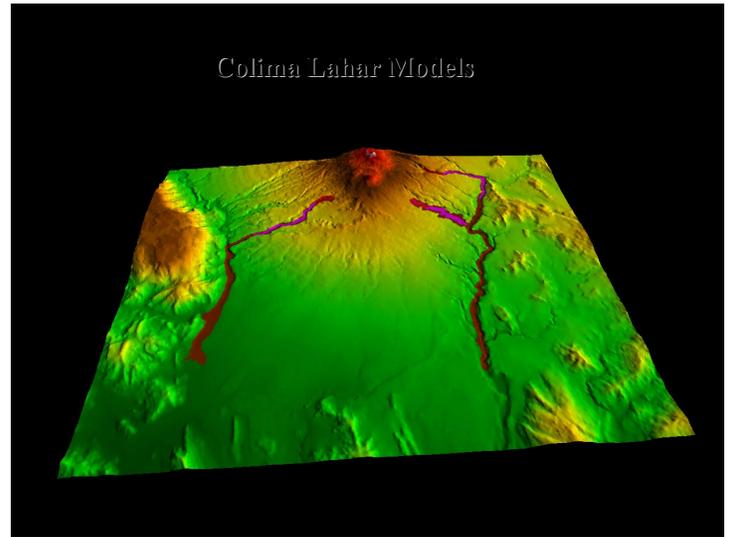
## Volcan Colima

- Most active volcano in Mexico
- Large volcanic debris avalanches and lahars occurred in the past
- Recurrence interval is about 2000 years for large events
- Recurrence interval for small lahars is about 100 years

Colima Lahar, Barranca La Lumbre, 1 June 2000



Colima Lahar Models



## Mount St. Helens Mudflows

- Followed major drainages
- Several types represented
- Present a large geologic hazard

